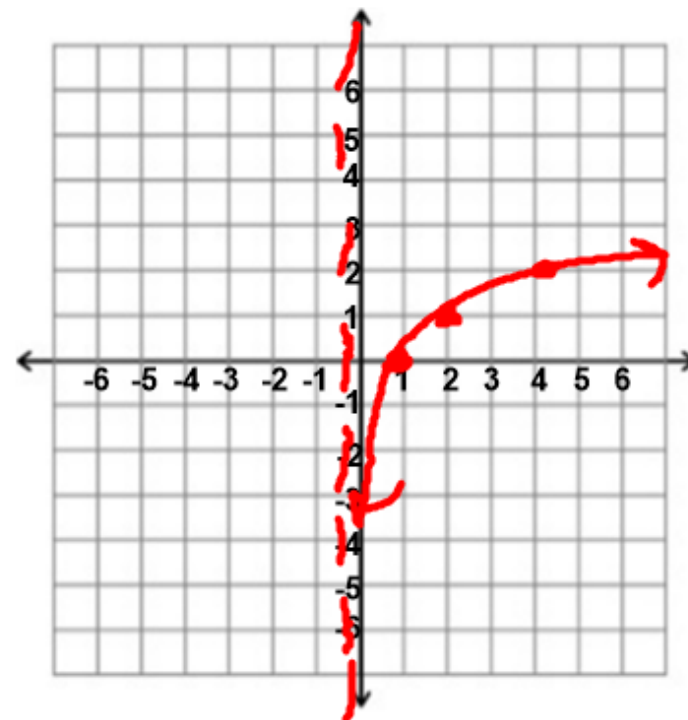
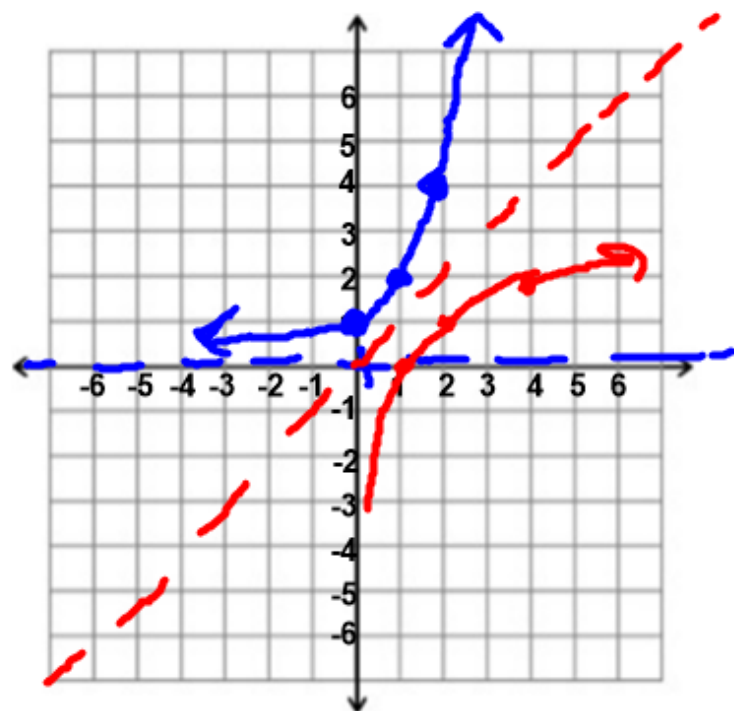


## Lesson 9.3: Graphing Logarithms

$$y = 2^x \xrightarrow{\text{Inverses}}$$

$$y = \log_2 x$$



HA:  $y = 0$

D:  $\mathbb{R}$

R:  $y > 0$

VA:  $x = 0$

D:  $x > 0$

R:  $\mathbb{R}$

## General Equation

$$y = a \log_b(x - h) + k$$

Vertical shift

y-distortion  
multiplying y's  
by a.

Vertical Asymptote:  $x = h$   
(Horizontal Shift  
opposite direction)

Key Points: \*

(1,0) and (b,1)

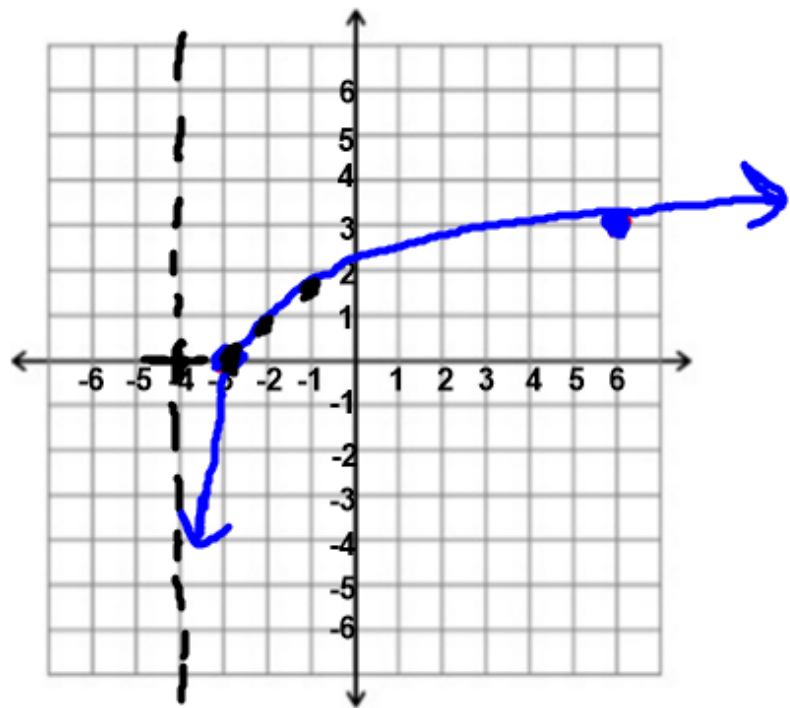
$$\log_b a = \frac{\log(a)}{\log(b)}$$

→ If you use Plug and Chug.

$$y = 3 \log(x + 4)$$

y-dist

(2) 4



VA:  $x = -4$

D:  $x > -4$

R:  $\mathbb{R}$

(1, 0)      (6, 1)

(1, 0)      (10, 1)

x3

x3

1, 0

10, 3

Plug and Chug Method

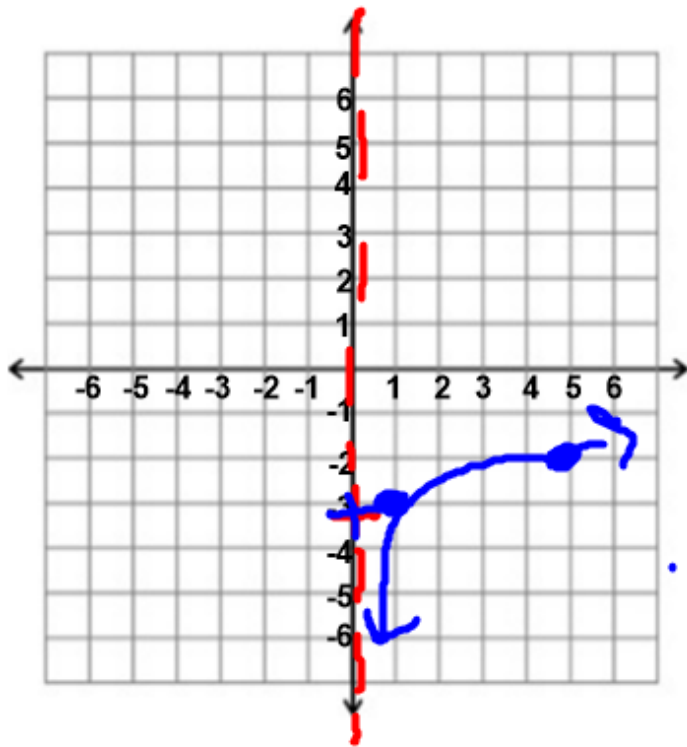
x	y
-3	0
-2	1
-1	1.4

$$y = \log_5 x - 3$$

Down 3

(1, 0)

(5, 1)



VA:  $x = 0$

D:  $x > 0$

R:  $\mathbb{R}$

Plug and Chug Method

x	y
1	$\log_5(1) - 3 = -3$
2	$\log_5(2) - 3 =$
3	$\log_5(3) - 3 =$

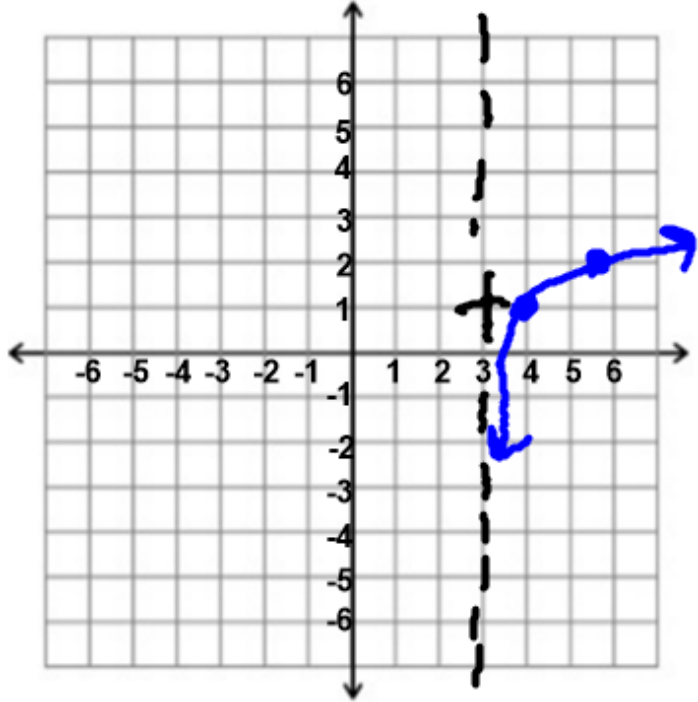
Change of Base

$$y = \ln(x - 3) + 1$$

(R) 3      up 1

(1, 0)

(6, 1)  
↓  
(2.7, 1)



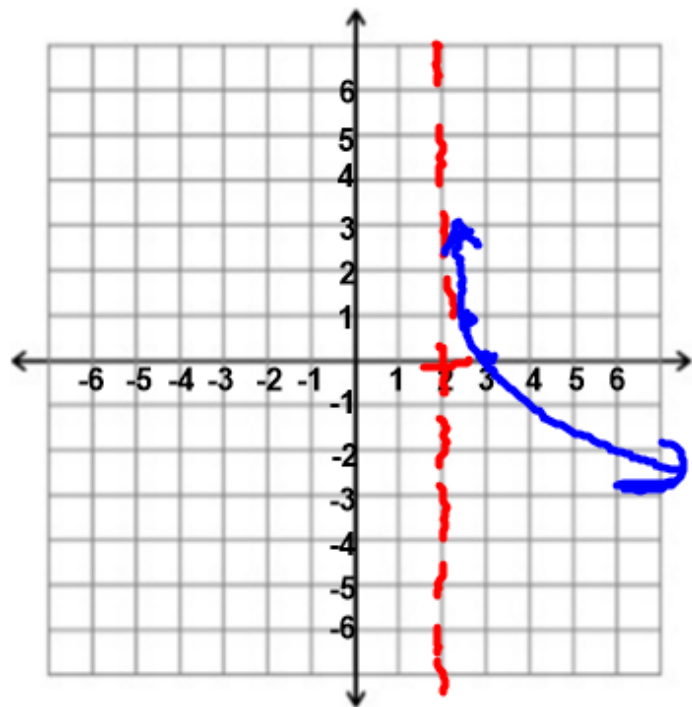
VA:  $x = 3$

D:  $x > 3$

R:  $\mathbb{R}$

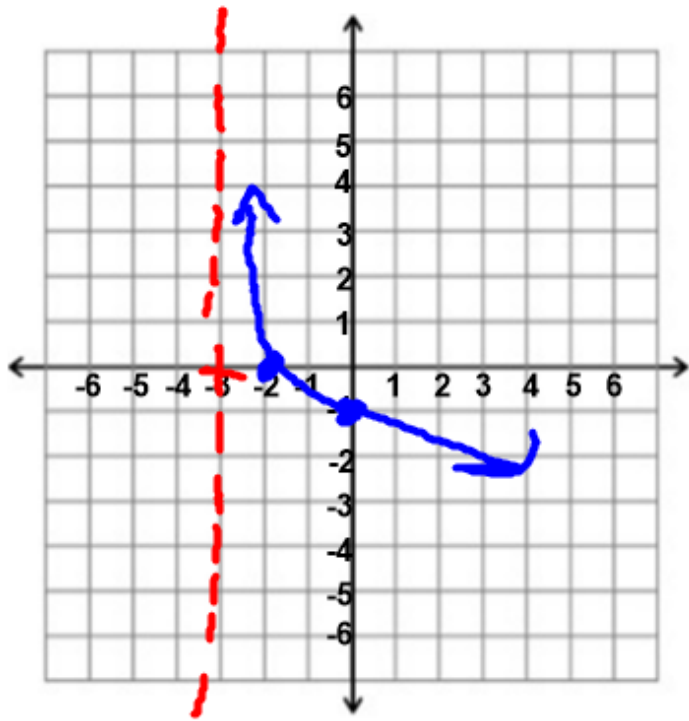
$$y = \log_{1/4}(x - 2)$$

$$(1, 0) \quad \left(\frac{1}{4}, 1\right)$$



$$y = -\log_3(x + 3)$$

$\swarrow$   
y-dist.



$$(1, 0)$$

$\downarrow$   
 $x - 1$

$$(1, 0)$$

$$(3, 1)$$

$x - 1$

$$(3, -1)$$

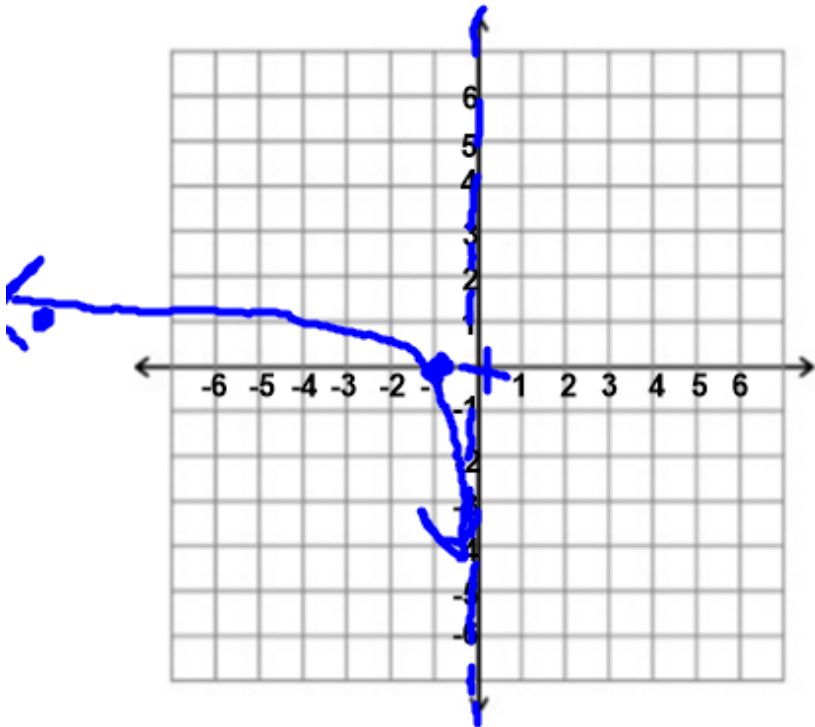
$$\text{VA: } x = -3$$

$$\text{D: } x > -3$$

$$\text{R: } \mathbb{R}$$

$$y = \log(-x)$$

$x$ -dist.



$$VA: x = 0$$

$$D: x < 0$$

$$R: \mathbb{R}$$

$$\begin{aligned} & (1, 0) \\ & \div -1 \\ & \downarrow \\ & (-1, 0) \end{aligned}$$

$$\begin{aligned} & (10, 1) \\ & \div -1 \\ & \downarrow \\ & (-10, 1) \end{aligned}$$